An Integrated Formal Methods Tool-Chain and its Application to Verifying a File System Model

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#### Skeleton

- Brief Introduction
- Tool-chain Scheme
- Point-free Specification and Allow Mapping
- Execution and proof chain (VDM++ and HOL)

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Conclusion and discussion

# **Brief Introduction**

The paper proposes a tool-chain and also a short case study for validation.

The tool-chain has the following requirements:

- 1. promote incremental development and verification of specifications;
- 2. be agile enough to encourage users to verify even the smallest unit of their specifications;
- be capable of producing immediate feedback to unveil problems;
- 4. be capable of performing fully automated consistency proofs;
- 5. be amenable to automatic code generation.

In addiction:

 The case study of the formal model for an abstract file system (following the Intel architecture).

#### **Tool-chain Scheme**



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Point-free Model - An abstract file system.



 Referential integrity: non existing files cannot be handled by applications.

 $\forall p \in Path, fh \in FileHandle : (\exists fd \in FileDescriptor :$ 

 $p(path) fd \land fd(table s) fh) \implies (\exists f \in File : p(fileStore s)f)$ 

 Paths closure: parent directories always exist and are indeed directories.

(fileStore s). Directory.  $id^{\circ}$ .  $fileType^{\circ} \subseteq dirName$ . (fileStore s)

. . . .

# Alloy Model

```
sig System {
  fileStore: Path -> lone File,
  table: FileHandle -> lone FileDescriptor }
abstract sig Path {dirName: one Path}
sig File {fileType : one FileType}
sig FileDescriptor {path: one Path}
sig FileHandle {}
```

And the Alloy model can be refined extending the path symbols and structure...

```
one sig Root extends Path
sig FileNames extends Path {}
pred ps[] {
   Reflexive[id[Root].dirName, Root]
   Acyclic[id[FileNames].dirName, FileNames] }
```

Lastly, after the model is validated can be translated to a... Can be translated to a...

# VDM++

What is VDM++?

 A language and a set of tools that allows proof obligations generation.

Here we need to refine the path data structure according to  $\mathsf{VDM}{++}...$ 

- However, model translation to VDM++ involves additional effort and increases the steepness of the learning curve.
- The outcome is a sizeable VDM++ model; the abstraction level is lowered, in order for the specification to become executable.

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# VDM++ to HOL

For each PO arising from the specification, the Overture proof system can yield three different results:

- the PO evaluates to true (discharged) no inconsistency found;
- the PO evaluates to false a design inconsistency exists;
- the PO evaluates to an unproven goal no conclusion from proof.

In the case that PO cannot be evaluated or is an unproved goal, we need to apply PF-Calculus techniques manually. This is clearly an hard step.

# Conclusion and discussion

Pros

- 1. The paper is well structured and presents an ambitious refinement scheme, using point free specifications.
- Given a PF-specification, we can convert PF-specifications to Alloy with a mechanized scheme, however, those refinements are very far from the first model. The conversion to VDM++ allows the generation of proof obligations to be proved in HOL. If cannot be proved it can be split in a point free fashion.
- 3. Making this steps in an automated way is a possible choice, and implies error freedom on translation but not on refinement.

Cons

1. The paper assumes that the reader is very comfortable with Alloy and VDM++.